

GCSE Higher Mathematics

Practice Test 4: Statistics

Instructions:

Answer all questions. Show your working clearly.
Calculators may be used unless stated otherwise.
Time allowed: 90 minutes

Section A: Advanced Averages and Spread

1. The table shows the distribution of video game completion times:

Time (hours)	Frequency
15-19	6
20-24	11
25-29	17
30-34	23
35-39	19
40-44	13
45-49	9
50-54	5

Calculate:

- The total number of players
 - An estimate of the mean completion time
 - The modal class
 - An estimate of the median completion time
 - An estimate of the range
2. For the data set: 24, 27, 30, 33, 36, 39, 42, 45, 48, 54
- Calculate the mean
 - Find the median and quartiles (Q1 and Q3)
 - Calculate the interquartile range
 - Calculate the standard deviation
 - Identify any outliers using the $1.5 \times \text{IQR}$ rule
3. Two data sets have the following properties:
- Set M: mean = 48, standard deviation = 9, $n = 28$
 - Set N: mean = 55, standard deviation = 14, $n = 32$
- Calculate the combined mean

- (b) Calculate the combined standard deviation
 - (c) Which set is more consistent? Explain.
 - (d) Calculate the coefficient of variation for each set
4. The scores of 48 students in a test are summarized:

$$\sum x = 3360, \sum x^2 = 240480$$

- (a) Calculate the mean score
- (b) Calculate the variance
- (c) Calculate the standard deviation
- (d) If 5 marks are added to each score, find the new mean and standard deviation

Section B: Histograms and Frequency Density

5. The histogram shows the distribution of flight delays:

[Imagine a histogram with: 0-15 min (density 4.2), 15-30 min (density 3.6), 30-45 min (density 2.8), 45-75 min (density 1.4), 75-120 min (density 0.8)]

- (a) Complete the frequency table
 - (b) Calculate the total number of flights
 - (c) Estimate the mean delay time
 - (d) Find the modal class
 - (e) What percentage of flights have delays over 45 minutes?
6. Draw a histogram for this data about book prices:

Price (£)	Frequency
5-10	25
10-15	40
15-18	21
18-22	24
22-28	18
28-35	14

- (a) Calculate the frequency density for each class
 - (b) Draw the histogram
 - (c) Estimate the median book price
 - (d) What fraction of books cost more than £18?
7. A histogram shows data with unequal class widths. The class 40-45 has frequency density 16 and the class 45-55 has frequency 80.
- (a) Find the frequency for the 40-45 class
 - (b) Find the frequency density for the 45-55 class
 - (c) If the total frequency is 400, suggest frequencies for other classes

Section C: Cumulative Frequency and Box Plots

8. The table shows the cumulative frequency of swimming lap times:

Time (seconds)	Cumulative Frequency
≤ 45	8
≤ 50	22
≤ 55	38
≤ 60	56
≤ 65	71
≤ 70	83
≤ 75	91
≤ 80	95

- Draw the cumulative frequency curve
- Find the median
- Find the quartiles Q1 and Q3
- Calculate the interquartile range
- Draw a box plot
- Estimate the 80th percentile

9. Two box plots show the distribution of commute times for two cities:

[Imagine box plots: City A (min 18, Q1 28, median 36, Q3 44, max 62), City B (min 22, Q1 32, median 40, Q3 48, max 66)]

Compare the distributions by commenting on:

- Central tendency (medians)
 - Spread (ranges and IQRs)
 - Shape and outliers
 - Which city has more variable commute times?
10. The cumulative frequency curve for download times (in seconds) passes through these points: (10, 0), (15, 14), (20, 32), (25, 48), (30, 61), (35, 72), (40, 78)
- Find the median download time
 - Find the quartiles
 - What percentage have download times between 18 seconds and 28 seconds?
 - Draw the corresponding box plot

Section D: Scatter Graphs and Correlation

11. The table shows data for 10 smartphones:

Storage (GB)	32	64	96	128	160	192	224	256	288	320
Price (£)	280	340	400	460	520	580	640	700	760	820

- Plot a scatter graph
- Describe the correlation
- Calculate the equation of the line of best fit
- Use your line to predict the price for 180GB storage

- (e) Estimate the storage for a phone priced at £600
 - (f) Calculate the correlation coefficient
12. The equation of a regression line is $y = 3.2x - 15$.
- (a) Interpret the gradient
 - (b) Interpret the y-intercept
 - (c) If $x = 25$, predict y
 - (d) If $y = 118$, estimate x
 - (e) State assumptions made when using this model
13. Classify these correlation coefficients and describe the relationships:
- (a) $r = 0.86$
 - (b) $r = -0.71$
 - (c) $r = 0.18$
 - (d) $r = -0.93$
 - (e) $r = 0.65$

Section E: Advanced Probability

14. A deck contains 8 hearts, 6 clubs, and 5 spades. Two cards are drawn without replacement.
- (a) Draw a tree diagram
 - (b) Find $P(\text{both hearts})$
 - (c) Find $P(\text{both same suit})$
 - (d) Find $P(\text{at least one club})$
 - (e) Find $P(\text{different suits})$
15. The probability that a router disconnects on any day is 0.12, independently of other days.
- (a) Find the probability it disconnects on exactly 3 out of 7 days
 - (b) Find the probability it disconnects on at least 4 out of 7 days
 - (c) Find the expected number of disconnections in 10 days
 - (d) In a 30-day month, find $P(\text{more than 5 disconnections})$
16. A driving test has 20 multiple choice questions, each with 3 options. A candidate guesses randomly.
- (a) Find $P(\text{correct answer on one question})$
 - (b) Find $P(\text{exactly 7 correct answers})$
 - (c) Find $P(\text{at least 14 correct answers})$
 - (d) Find the expected number of correct answers
 - (e) Find the most likely number of correct answers
17. Events G and H are such that $P(G) = 0.55$, $P(H) = 0.65$, and $P(G \cap H) = 0.33$.
- (a) Find $P(G \cap H)$
 - (b) Find $P(G')$
 - (c) Find $P(G \cup H)$
 - (d) Find $P(H \cap G)$
 - (e) Are G and H independent? Justify your answer

Section F: Conditional Probability and Independence

18. A survey of 300 students about course preferences gives:
- 180 prefer Mathematics
 - 135 prefer Science
 - 75 prefer both subjects
- (a) Draw a Venn diagram
- (b) Find $P(\text{prefers Mathematics} \mid \text{prefers Science})$
- (c) Find $P(\text{prefers Science} \mid \text{prefers Mathematics})$
- (d) Find $P(\text{prefers exactly one subject})$
- (e) Are the subject preferences independent? Explain
19. In a food processing plant, 65% of products are packed by Line 1 and 35% by Line 2. Line 1 produces 2% contaminated products, Line 2 produces 5% contaminated products.
- (a) Draw a tree diagram
- (b) Find the probability a product is contaminated
- (c) If a product is contaminated, find the probability it came from Line 1
- (d) If a product is not contaminated, find the probability it came from Line 2
20. A box contains 14 square tiles numbered 1-14 and 10 circular tiles numbered 1-10. A tile is drawn at random.
- (a) Find $P(\text{square and multiple of 3})$
- (b) Find $P(\text{circular} \mid \text{number less than 6})$
- (c) Find $P(\text{number} < 10)$
- (d) Are shape and number size independent?
21. A security scan is 94% accurate for threats and 97% accurate for non-threats. 1.5% of items contain threats.
- (a) Find the probability of a positive scan result
- (b) If an item triggers the scan, find the probability it contains a threat
- (c) If an item passes the scan, find the probability it's safe
- (d) Comment on the effectiveness of the security scan

Section G: Hypothesis Testing and Sampling

22. A lottery scratch card is suspected of having a higher win rate than advertised. Out of 40 cards tested, 12 are winners.
- (a) State the null and alternative hypotheses (advertised rate is 20%)
- (b) Calculate the probability of getting 12 or more winners if the rate is 20%
- (c) At the 5% significance level, is there evidence the win rate is higher?
- (d) What would be a Type I error in this context?
23. A sample of 55 laptop batteries has mean lifespan 840 hours and standard deviation 95 hours.
- (a) Calculate a 95% confidence interval for the population mean
- (b) Interpret your confidence interval

- (c) What assumptions are made?
- (d) How would the interval change with a 90% confidence level?
24. A delivery service claims 96% on-time delivery. In a sample of 200 deliveries, 188 are on time.
- (a) Test at 5% level whether the claim is justified
- (b) Calculate the critical value
- (c) State your conclusion
- (d) What is the p-value for this test?

Section H: Problem Solving and Integration

25. A coffee shop records customer service times over 180 transactions. The data shows:
- Mean = 4.2 minutes
 - Standard deviation = 1.1 minutes
 - Distribution is approximately normal
- (a) Find $P(\text{service time} < 6 \text{ minutes})$
- (b) Find the service time exceeded by only 8% of customers
- (c) What percentage of transactions take between 3 and 5.5 minutes?
- (d) If the shop serves 400 customers daily, estimate complaints (assuming complaints when service > 5.5 minutes)
26. A manufacturing process samples 12 components every 30 minutes. Over 10 sampling periods, the number of defective components found was: 1, 0, 2, 1, 3, 0, 1, 2, 0, 1.
- (a) Calculate the mean and standard deviation
- (b) Test whether the defect rate exceeds 6%
- (c) Create a control chart with warning limits
- (d) Comment on process stability
27. Compare these three retirement fund options over 10 years:
- Fund X: Mean return 6%, standard deviation 8%
 - Fund Y: Mean return 9%, standard deviation 14%
 - Fund Z: Mean return 4%, standard deviation 5%
- (a) Calculate the coefficient of variation for each
- (b) Which offers the best risk-adjusted return?
- (c) Using normal distribution, find $P(\text{return} < 0\%)$ for each fund
- (d) Recommend an option for a risk-neutral investor
28. A language school studies the relationship between practice hours and test scores. The correlation is 0.79.
- (a) What does this correlation suggest?
- (b) If practice hours have mean 15 and standard deviation 6, and test scores have mean 78 and standard deviation 18, find the regression equation
- (c) Predict the test score for a student practicing 20 hours
- (d) Calculate the coefficient of determination and interpret it

29. Design a statistical investigation to determine if online learning is as effective as classroom learning:
- (a) State hypotheses
 - (b) Describe the sampling method
 - (c) Identify variables and potential confounding factors
 - (d) Outline the analysis plan
 - (e) Discuss limitations and assumptions

Answer Space

Use this space for your working and answers.

END OF TEST

Total marks: 100

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