

A Level Mechanics

Practice Test 3: Momentum and Impulse

Instructions:

Answer all questions. Show your working clearly.

Calculators may be used unless stated otherwise.

Draw diagrams where appropriate to illustrate your solutions.

Time allowed: 2 hours 25 minutes

Section A: Complex Momentum Systems [30 marks]

Question 1 [20 marks] Four particles are arranged in a system: particle A (mass 2 kg, velocity 8 m/s east), particle B (mass 3 kg, velocity 6 m/s west), particle C (mass 1.5 kg, velocity 10 m/s north), and particle D (mass 2.5 kg, velocity 4 m/s south).

- (a) Calculate the total momentum of the system (magnitude and direction). [6 marks]
- (b) Find the velocity of the center of mass of the system. [4 marks]
- (c) If all particles suddenly stick together, find their common velocity. [4 marks]
- (d) Calculate the kinetic energy before and after they stick together. [4 marks]
- (e) Determine what fraction of the original kinetic energy is lost. [2 marks]

Question 2 [10 marks] A space probe of mass 800 kg ejects a fuel pod of mass 200 kg backward at 50 m/s relative to the probe. Initially, both were moving together at 15 m/s.

- (a) Calculate the velocity of the probe after ejecting the fuel pod. [4 marks]
- (b) Find the velocity of the fuel pod relative to a stationary observer. [3 marks]
- (c) Calculate the change in kinetic energy of the system. [3 marks]

Section B: Advanced Collision Dynamics [35 marks]

Question 3 [20 marks] A ball of mass 1.8 kg moving at 15 m/s collides with a ball of mass 2.2 kg moving at 10 m/s in the opposite direction. The coefficient of restitution is 0.75.

- (a) Calculate the velocities of both balls after collision. [8 marks]
- (b) Find the impulse experienced by each ball. [6 marks]
- (c) Calculate the kinetic energy lost in the collision. [4 marks]
- (d) Determine the percentage of kinetic energy retained. [2 marks]

Question 4 [15 marks] A Newton's cradle consists of five identical balls, each of mass 0.05 kg, suspended by strings. Ball 1 is pulled back and released, striking the stationary balls with velocity 3 m/s.

- (a) Assuming elastic collisions, determine what happens after ball 1 strikes the group. [5 marks]
- (b) Calculate the velocity of ball 5 immediately after the collision sequence. [3 marks]
- (c) If ball 5 swings to a height of 0.4 m, verify energy conservation. [4 marks]
- (d) Explain why only ball 5 moves significantly after the collision. [3 marks]

Section C: Variable Force Analysis [25 marks]

Question 5 [15 marks] A hammer strikes a nail with a force that varies according to $F = 500t - 2000t^2$ N, where t is in seconds. The hammer has mass 0.8 kg and initial velocity 4 m/s.

- (a) Calculate the impulse delivered during the time interval from $t = 0$ to $t = 0.2$ s. [4 marks]
- (b) Find the velocity of the hammer after 0.2 seconds. [3 marks]
- (c) Determine when the force reaches its maximum value. [3 marks]
- (d) Calculate the maximum force and the impulse delivered up to this point. [5 marks]

Question 6 [10 marks] A tennis ball bounces on the ground with coefficient of restitution 0.85. It hits the ground with velocity 18 m/s downward.

- (a) Calculate the velocity immediately after bouncing. [2 marks]
- (b) If the contact time is 0.005 seconds and the ball has mass 0.057 kg, find the average force during contact. [4 marks]
- (c) Determine the impulse from the ground on the ball. [2 marks]
- (d) Calculate the height the ball reaches after bouncing. [2 marks]

Section D: Multi-Dimensional Collision Problems [30 marks]

Question 7 [18 marks] A hockey puck of mass 0.16 kg slides across ice at 12 m/s and collides with a stationary puck of mass 0.18 kg. After collision, the first puck moves at 6 m/s at 40° to its original direction.

- (a) Find the velocity components of the first puck after collision. [3 marks]
- (b) Using conservation of momentum, calculate the velocity of the second puck. [6 marks]
- (c) Determine if this collision is elastic by checking energy conservation. [5 marks]
- (d) Calculate the coefficient of restitution for this collision. [4 marks]

Question 8 [12 marks] Two cars collide at an intersection. Car A (mass 1400 kg) traveling north at 20 m/s collides with car B (mass 1600 kg) traveling east at 15 m/s. They stick together after collision.

- (a) Calculate the velocity of the combined cars immediately after collision. [5 marks]
- (b) Find the direction of motion after collision. [3 marks]
- (c) Calculate the kinetic energy lost in the collision. [4 marks]

Section E: Explosion and Fragmentation [20 marks]

Question 9 [20 marks] A grenade of mass 2 kg is thrown horizontally at 8 m/s and explodes at the highest point of its trajectory into three fragments. Fragment A (mass 0.6 kg) flies horizontally at 25 m/s in the original direction, fragment B (mass 0.8 kg) flies at 30 m/s at 60° above the horizontal in the original direction.

- (a) Calculate the velocity of the grenade just before explosion. [2 marks]
- (b) Find the momentum of the grenade just before explosion. [2 marks]
- (c) Calculate the velocity components of fragments A and B. [4 marks]
- (d) Using conservation of momentum, find the velocity of fragment C. [6 marks]
- (e) Calculate the total kinetic energy released in the explosion. [4 marks]
- (f) Determine the impulse experienced by fragment A during explosion. [2 marks]

Section F: Advanced Applications [25 marks]

Question 10 [15 marks] A spacecraft of mass 2000 kg approaches a space station at 50 m/s. To dock safely, it fires retro-rockets that eject gas at 3000 m/s relative to the spacecraft at a rate of 8 kg/s.

- (a) Calculate the thrust force produced by the retro-rockets. [3 marks]
- (b) Find the initial deceleration of the spacecraft. [3 marks]
- (c) If the rockets fire for 12 seconds, calculate the final velocity using the rocket equation. [6 marks]
- (d) Determine the total impulse delivered by the rockets. [3 marks]

Question 11 [10 marks] A ballistic pendulum consists of a wooden block of mass 5 kg suspended by strings. A bullet of mass 0.025 kg moving horizontally embeds in the block, causing it to swing to a maximum angle of 30° from vertical.

- (a) Calculate the velocity of the block immediately after the bullet embeds. [4 marks]
- (b) Find the initial velocity of the bullet. [3 marks]
- (c) Calculate the kinetic energy lost when the bullet embeds. [3 marks]

Section G: Complex System Analysis [15 marks]

Question 12 [15 marks] A chain of mass 12 kg and length 4 m lies on a frictionless table with 1 m hanging over the edge. The chain is released from rest.

- (a) When 2 m of chain has fallen off the table, calculate the velocity of the chain using energy methods. [4 marks]
- (b) Find the momentum of the entire chain at this instant. [3 marks]
- (c) Calculate the impulse delivered to the chain by gravity from release until 2 m has fallen. [4 marks]
- (d) Determine the average force exerted by the table on the remaining chain during this time. [4 marks]

Physics Data and Formulae**Momentum and Impulse:**

$$\text{Momentum: } \vec{p} = m\vec{v}$$

$$\text{Impulse: } \vec{J} = \vec{F}\Delta t = \Delta\vec{p}$$

$$\text{For variable force: } J = \int F dt$$

$$\text{Conservation of momentum: } \sum \vec{p}_{\text{before}} = \sum \vec{p}_{\text{after}}$$

Center of Mass:

$$\text{Velocity of center of mass: } v_{cm} = \frac{\sum m_i v_i}{\sum m_i}$$

$$\text{Position of center of mass: } x_{cm} = \frac{\sum m_i x_i}{\sum m_i}$$

Collision Formulas:

$$\text{Elastic collision (1D): } v'_1 = \frac{(m_1 - m_2)v_1 + 2m_2v_2}{m_1 + m_2}$$

$$v'_2 = \frac{(m_2 - m_1)v_2 + 2m_1v_1}{m_1 + m_2}$$

$$\text{Perfectly inelastic: } v' = \frac{m_1v_1 + m_2v_2}{m_1 + m_2}$$

Coefficient of Restitution:

$$e = \frac{\text{speed of separation}}{\text{speed of approach}}$$

$$\text{For direct collision: } e = \frac{v'_2 - v'_1}{v_1 - v_2}$$

Rocket Equation:

$$v = v_0 + v_{rel} \ln \left(\frac{m_0}{m} \right)$$

$$\text{Thrust: } F = \frac{dm}{dt} \times v_{rel}$$

Energy Relations:

$$\text{Kinetic energy: } E_k = \frac{1}{2}mv^2$$

$$\text{Gravitational potential energy: } E_p = mgh$$

$$\text{Conservation of energy: } E_{\text{initial}} = E_{\text{final}}$$

Pendulum Relations:

$$\text{For pendulum: } h = l(1 - \cos \theta)$$

$$v = \sqrt{2gl(1 - \cos \theta)}$$

Vector Analysis:

$$\text{Magnitude: } |\vec{v}| = \sqrt{v_x^2 + v_y^2}$$

$$\text{Direction: } \tan \theta = \frac{v_y}{v_x}$$

$$\text{Components: } v_x = v \cos \theta, v_y = v \sin \theta$$

Constants:

$$\text{Acceleration due to gravity: } g = 9.8 \text{ m/s}^2$$

END OF TEST

Total marks: 180

Grade boundaries: A* 162, A 144, B 126, C 108, D 90, E 72

For more resources and practice materials, visit:
stepupmaths.co.uk