

# GCSE Foundation Mathematics

## Practice Test 5: Geometry and Measures

### Instructions:

Answer all questions. Show your working clearly.

Calculators may be used unless stated otherwise.

Time allowed: 90 minutes

### Section A: Angles

- Classify these angles as acute, obtuse, or reflex:
  - $67^\circ$
  - $128^\circ$
  - $310^\circ$
  - $18^\circ$
  - $247^\circ$
  - $81^\circ$
- Find the missing angles:
  - Two angles on a straight line are  $124^\circ$  and  $x^\circ$ . Find  $x$ .
  - Three angles around a point are  $118^\circ$ ,  $97^\circ$ , and  $y^\circ$ . Find  $y$ .
  - Two angles are vertically opposite. One angle is  $53^\circ$ . Find the other angle.
- In a triangle, two angles are  $64^\circ$  and  $71^\circ$ . Find the third angle.
- The angles in a triangle are in the ratio  $2 : 5 : 8$ . Find the size of each angle.
- Find the missing angles in these triangles:
  - An isosceles triangle with base angles of  $x^\circ$  and vertex angle of  $70^\circ$
  - An equilateral triangle (all angles equal)
  - A right-angled triangle with one angle of  $73^\circ$

### Section B: Polygons and Angle Rules

- Find the sum of interior angles for:
  - A hexagon (6 sides)
  - An octagon (8 sides)
  - A decagon (10 sides)
  - A 15-sided polygon

7. Find the size of each interior angle in:
- (a) A regular nonagon
  - (b) A regular dodecagon
  - (c) A regular pentagon
  - (d) A regular hexagon
8. Find the size of each exterior angle in:
- (a) A regular nonagon
  - (b) A regular dodecagon
  - (c) A regular 15-sided polygon
  - (d) A regular octagon
9. A regular polygon has an exterior angle of  $18^\circ$ . How many sides does it have?
10. In a quadrilateral, three angles are  $73^\circ$ ,  $119^\circ$ , and  $91^\circ$ . Find the fourth angle.
11. A regular polygon has an interior angle of  $162^\circ$ . Find:
- (a) The exterior angle
  - (b) The number of sides

## Section C: Properties of Shapes

12. State the properties of these quadrilaterals:
- (a) Rhombus (sides, angles, diagonals)
  - (b) Parallelogram (sides, angles, diagonals)
  - (c) Square (sides, angles, diagonals)
  - (d) Kite (sides, angles, diagonals)
13. How many lines of symmetry do these shapes have?
- (a) Regular decagon
  - (b) Kite
  - (c) Regular pentagon
  - (d) Rectangle
  - (e) Equilateral triangle
  - (f) Rhombus
14. What is the order of rotational symmetry for:
- (a) Regular decagon
  - (b) Regular octagon
  - (c) Rectangle
  - (d) Square
15. Name these 3D shapes:
- (a) 2 circular faces and 1 curved surface
  - (b) 1 octagonal base and 8 triangular faces
  - (c) 7 faces: 2 pentagonal and 5 rectangular

- (d) 1 circular base and 1 curved surface meeting at a point
  - (e) 20 triangular faces
16. How many faces, edges, and vertices do these shapes have?
- (a) Octagonal prism
  - (b) Pentagonal pyramid
  - (c) Triangular prism
  - (d) Cube

## Section D: Transformations

17. Describe the transformation that maps:
- (a) Shape A to Shape B (rotation  $90^\circ$  anticlockwise about origin)
  - (b) Shape B to Shape C (reflection in line  $y = -x$ )
  - (c) Shape C to Shape D (translation 6 units right, 3 units up)
  - (d) Shape D to Shape E (enlargement scale factor  $\frac{3}{2}$ , centre origin)
18. A point P(7, 4) is transformed. Find the image coordinates after:
- (a) Reflection in the x-axis
  - (b) Reflection in the y-axis
  - (c) Reflection in the line  $y = x$
  - (d) Translation by vector  $\begin{pmatrix} -5 \\ 3 \end{pmatrix}$
19. A quadrilateral has vertices at A(3, 2), B(7, 2), C(7, 6), and D(3, 6). Find the coordinates after:
- (a) Rotation  $180^\circ$  about the origin
  - (b) Enlargement scale factor  $\frac{2}{3}$ , centre origin
  - (c) Translation by vector  $\begin{pmatrix} 4 \\ -3 \end{pmatrix}$
20. A shape is enlarged by scale factor  $\frac{3}{4}$ . If the original area is  $64 \text{ cm}^2$ , what is the new area?
21. Shape A is enlarged to Shape B with scale factor  $\frac{2}{3}$ . If Shape A has a perimeter of 18 cm, what is the perimeter of Shape B?

## Section E: Perimeter and Area

22. Calculate the perimeter of these shapes:
- (a) Rectangle: length 17 cm, width 11 cm
  - (b) Square: side length 15 cm
  - (c) Triangle: sides 13 cm, 14 cm, 15 cm
  - (d) Regular decagon: side length 3.5 cm
23. Calculate the area of these shapes:
- (a) Rectangle: length 19 cm, width 13 cm
  - (b) Square: side length 17 cm
  - (c) Triangle: base 22 cm, height 11 cm

- (d) Parallelogram: base 16 cm, height 9 cm
24. Calculate the area and circumference of circles with:
- (a) Radius 9 cm
  - (b) Diameter 15 cm
  - (c) Radius 6.5 cm
  - (d) Diameter 28 cm
25. A rectangular sports field is 45 m long and 30 m wide. Find:
- (a) The perimeter
  - (b) The area
  - (c) The cost of boundary marking at £8 per metre
  - (d) The cost of maintenance at £4 per  $\text{m}^2$
26. Find the area of these compound shapes:
- (a) A rectangle 18 cm by 12 cm with a rectangle 6 cm by 4 cm removed from the centre
  - (b) A T-shape made from two rectangles: 15 cm by 4 cm and 6 cm by 8 cm overlapping
  - (c) A quarter circle with radius 8 cm attached to a square 8 cm by 8 cm

## Section F: Volume and Surface Area

27. Calculate the volume of these prisms:
- (a) Cuboid: length 14 cm, width 9 cm, height 8 cm
  - (b) Cube: side length 11 cm
  - (c) Triangular prism: triangular face area  $30 \text{ cm}^2$ , length 8 cm
  - (d) Cylinder: radius 7 cm, height 14 cm
28. Calculate the surface area of:
- (a) Cube: side length 9 cm
  - (b) Cuboid: length 16 cm, width 11 cm, height 8 cm
  - (c) Cylinder: radius 7 cm, height 12 cm
29. A cylindrical chemical tank has radius 4.5 m and height 10 m. Find:
- (a) The volume in  $\text{m}^3$
  - (b) The volume in litres ( $1 \text{ m}^3 = 1000 \text{ litres}$ )
  - (c) The curved surface area
  - (d) The total surface area
30. A cube has volume  $729 \text{ cm}^3$ . Find:
- (a) The side length
  - (b) The surface area
31. A rectangular reservoir is 25 m long, 15 m wide, and 4 m deep. Find:
- (a) The volume of water needed to fill it
  - (b) The area of the bottom
  - (c) The area of the four walls

## Section G: Pythagoras' Theorem

32. Use Pythagoras' theorem to find the missing side in these right-angled triangles:
- (a) Two shorter sides are 15 cm and 20 cm. Find the hypotenuse.
  - (b) Hypotenuse is 41 cm, one side is 40 cm. Find the other side.
  - (c) Two shorter sides are 16 cm and 30 cm. Find the hypotenuse.
  - (d) Hypotenuse is 37 cm, one side is 35 cm. Find the other side.
33. A wire of length 10 m is stretched from the top of a 9.5 m pole to a point on the ground. How far is this point from the base of the pole?
34. A rectangle has length 35 cm and width 12 cm. Find the length of its diagonal.
35. Find the distance between these pairs of points:
- (a) (0, 0) and (15, 20)
  - (b) (5, 7) and (17, 12)
  - (c) (-4, 1) and (8, 16)
36. A right-angled triangle has legs of length  $x$  cm and  $(x + 9)$  cm, and hypotenuse  $(x + 15)$  cm. Find the value of  $x$ .
37. Determine whether these triangles are right-angled:
- (a) Sides 14 cm, 48 cm, 50 cm
  - (b) Sides 16 cm, 30 cm, 35 cm
  - (c) Sides 33 cm, 56 cm, 65 cm
  - (d) Sides 28 cm, 45 cm, 53 cm

## Section H: Problem Solving

38. A circular plaza has radius 8 m. A decorative border of width 3 m surrounds the plaza. Find:
- (a) The area of the plaza
  - (b) The area of the border
  - (c) The total area including the border
39. A regular 15-sided polygon has perimeter 75 cm. Find:
- (a) The length of each side
  - (b) Each interior angle
  - (c) Each exterior angle
40. A cylindrical water heater has radius 8 cm and height 25 cm. Find:
- (a) How much water it can hold (volume)
  - (b) The area of metal needed to make it (surface area)
  - (c) The cost of metal at £0.05 per  $\text{cm}^2$
41. Triangle JKL is isosceles with  $JK = JL$ . Angle  $KJL = 25^\circ$ . Find angles JKL and JLK.
42. A regular hexagon and a circle have the same perimeter. If the hexagon has side length 6 cm, find the radius of the circle.

43. A triangle has vertices at A(4, 5), B(12, 5), and C(8, 17). Find:
- (a) The length of each side
  - (b) The perimeter
  - (c) The area
  - (d) Whether the triangle is right-angled
44. A cone has base radius 12 cm and slant height 20 cm. Find:
- (a) The vertical height
  - (b) The volume
  - (c) The curved surface area
45. A warehouse floor is 15 m by 12 m. Square tiles of side 60 cm are used to cover the floor. How many tiles are needed?

**Answer Space**

Use this space for your working and answers.

**END OF TEST**

Total marks: 100

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