

A Level Mechanics

Practice Test 1: Gravitational Fields

Instructions:

Answer all questions. Show your working clearly.
Calculators may be used unless stated otherwise.
Draw diagrams where appropriate to illustrate your solutions.
Time allowed: 2 hours 45 minutes

Section A: Newton's Law of Universal Gravitation [30 marks]

Question 1 [12 marks]

- (a) State Newton's Law of Universal Gravitation in words. [3 marks]
- (b) Write the mathematical expression for the gravitational force between two point masses. [2 marks]
- (c) Define the gravitational constant G , stating its value and units. [3 marks]
- (d) Explain why gravitational forces are always attractive, never repulsive. [2 marks]
- (e) State two conditions under which Newton's law applies to extended objects like planets. [2 marks]

Question 2 [18 marks] Two point masses of 800 kg and 1200 kg are placed 6.0 m apart in space.

- (a) Calculate the gravitational force between these masses. [4 marks]
- (b) If the distance between them is doubled to 12.0 m, calculate the new gravitational force. [3 marks]
- (c) What happens to the gravitational force if one mass is tripled while keeping the distance constant? [3 marks]
- (d) Calculate the gravitational force between Earth (mass 5.97×10^{24} kg) and a 70 kg person standing on its surface. Take Earth's radius as 6.37×10^6 m. [4 marks]
- (e) Compare this force with the person's weight calculated using $g = 9.81 \text{ m/s}^2$. [2 marks]
- (f) Explain why these two values should be the same. [2 marks]

Section B: Gravitational Field Strength [35 marks]

Question 3 [15 marks]

- (a) Define gravitational field strength and state its SI units. [3 marks]
- (b) Write the equation that relates gravitational field strength to gravitational force. [2 marks]

- (c) Show that for a point mass M , the gravitational field strength at distance r is given by $g = GM/r^2$. [4 marks]
- (d) Explain why gravitational field strength is a vector quantity. [2 marks]
- (e) Describe how gravitational field strength varies with distance from a point mass. [2 marks]
- (f) Sketch a graph showing how g varies with distance r from the center of a uniform sphere. [2 marks]

Question 4 [20 marks] The Moon has mass 7.35×10^{22} kg and radius 1.74×10^6 m.

- (a) Calculate the gravitational field strength on the Moon's surface. [4 marks]
- (b) Find the gravitational field strength at a height of 500 km above the Moon's surface. [4 marks]
- (c) An astronaut has mass 85 kg. Calculate their weight on the Moon's surface. [3 marks]
- (d) Compare this with their weight on Earth's surface. [3 marks]
- (e) At what height above the Moon's surface would the gravitational field strength be half its surface value? [4 marks]
- (f) Calculate the gravitational field strength at the center of the Moon. Explain your answer. [2 marks]

Section C: Gravitational Potential Energy [40 marks]

Question 5 [18 marks]

- (a) Define gravitational potential energy. [2 marks]
- (b) Explain why we choose gravitational potential energy to be zero at infinite separation. [3 marks]
- (c) Derive the expression $U = -GMm/r$ for the gravitational potential energy of mass m at distance r from mass M . [6 marks]
- (d) Explain why gravitational potential energy is negative. [3 marks]
- (e) Show that the change in gravitational potential energy equals the negative of the work done by the gravitational force. [4 marks]

Question 6 [22 marks] A satellite of mass 1500 kg orbits Earth at a height of 800 km above the surface.

- (a) Calculate the satellite's distance from Earth's center. [2 marks]
- (b) Find the gravitational potential energy of the satellite in this orbit. [4 marks]
- (c) Calculate the satellite's gravitational potential energy when on Earth's surface. [3 marks]
- (d) Determine the change in potential energy required to move the satellite from Earth's surface to its orbital position. [3 marks]
- (e) Calculate the minimum work that must be done to move the satellite to this orbit. [2 marks]
- (f) If the satellite moves to a higher orbit at 1200 km altitude, calculate the additional change in potential energy required. [4 marks]
- (g) What is the escape velocity from Earth's surface? [4 marks]

Section D: Gravitational Potential [25 marks]**Question 7 [12 marks]**

- (a) Define gravitational potential and state its SI units. **[3 marks]**
- (b) Write the relationship between gravitational potential V and gravitational potential energy U . **[2 marks]**
- (c) Show that the gravitational potential due to a point mass M at distance r is $V = -GM/r$. **[3 marks]**
- (d) Explain the relationship between gravitational field strength and gravitational potential. **[2 marks]**
- (e) Why is gravitational potential a scalar quantity while gravitational field strength is a vector? **[2 marks]**

Question 8 [13 marks]

- (a) Calculate the gravitational potential at Earth's surface. **[3 marks]**
- (b) Find the gravitational potential at a height of 1000 km above Earth's surface. **[4 marks]**
- (c) Calculate the potential difference between these two positions. **[2 marks]**
- (d) A 2.0 kg mass moves from Earth's surface to the 1000 km height. Calculate the change in potential energy. **[2 marks]**
- (e) Verify your answer using the potential difference and the definition of potential. **[2 marks]**

Section E: Orbital Motion [35 marks]**Question 9 [18 marks]**

- (a) For a satellite in circular orbit, what force provides the centripetal force? **[2 marks]**
- (b) Derive the expression $v = (GM/r)^{1/2}$ for circular orbital velocity. **[5 marks]**
- (c) Show that the orbital period is given by $T = 2\pi(r^3/GM)^{1/2}$. **[4 marks]**
- (d) Explain why orbital velocity decreases as orbital radius increases. **[3 marks]**
- (e) For a satellite in circular orbit, derive the relationship between kinetic energy and potential energy. **[4 marks]**

Question 10 [17 marks] A satellite orbits Earth at a height of 600 km above the surface in a circular orbit.

- (a) Calculate the orbital radius from Earth's center. **[2 marks]**
- (b) Find the orbital velocity of the satellite. **[4 marks]**
- (c) Calculate the orbital period in hours. **[4 marks]**
- (d) Determine the centripetal acceleration of the satellite. **[3 marks]**
- (e) For a satellite of mass 2000 kg in this orbit, calculate:
 - (i) The kinetic energy. **[2 marks]**
 - (ii) The gravitational potential energy. **[2 marks]**

Section F: Geostationary Satellites and Applications [25 marks]

Question 11 [15 marks]

- (a) State the conditions required for a geostationary satellite orbit. [3 marks]
- (b) Calculate the orbital radius for a geostationary satellite above Earth's center. [5 marks]
- (c) Find the height of a geostationary satellite above Earth's surface. [2 marks]
- (d) Calculate the orbital velocity of a geostationary satellite. [3 marks]
- (e) Explain why geostationary satellites cannot be placed in polar orbits. [2 marks]

Question 12 [10 marks] Compare satellites in different Earth orbits:

- (a) Calculate the orbital period for a satellite at height 400 km (Low Earth Orbit). [4 marks]
- (b) Find the orbital velocity for this satellite. [3 marks]
- (c) Compare the orbital velocities of satellites in Low Earth Orbit (400 km) and geostationary orbit. [2 marks]
- (d) State one advantage and one disadvantage of Low Earth Orbit compared to geostationary orbit. [1 mark]

Section G: Energy and Escape Velocity [20 marks]

Question 13 [12 marks]

- (a) Define escape velocity. [2 marks]
- (b) Derive the expression $v_e = (2GM/r)^{1/2}$ for escape velocity from the surface of a planet. [5 marks] Calculate the escape velocity from Earth's surface. [2 marks]
- (c) Calculate the escape velocity from the Moon's surface. [2 marks]

Question 14 [8 marks] A rocket is launched vertically from Earth's surface with an initial speed of 8.0 km/s.

- (a) Will this rocket escape Earth's gravitational field? Justify your answer. [3 marks]
- (b) Calculate the maximum height reached by the rocket. [5 marks]

Physics Data and Formulae

Gravitational Force:

$$\text{Newton's Law: } F = \frac{Gm_1m_2}{r^2}$$

Gravitational Field:

$$\text{Field strength: } g = \frac{F}{m} = \frac{GM}{r^2}$$

$$\text{Field-potential relationship: } g = -\frac{dV}{dr}$$

Gravitational Potential Energy and Potential:

$$\text{Potential energy: } U = -\frac{GMm}{r}$$

$$\text{Potential: } V = \frac{U}{m} = -\frac{GM}{r}$$

Orbital Motion:

$$\text{Circular orbital velocity: } v = \sqrt{\frac{GM}{r}}$$

$$\text{Orbital period: } T = 2\pi\sqrt{\frac{r^3}{GM}}$$

$$\text{Escape velocity: } v_e = \sqrt{\frac{2GM}{r}}$$

Energy in Orbits:

$$\text{Kinetic energy: } KE = \frac{1}{2}mv^2 = \frac{GMm}{2r}$$

$$\text{Potential energy: } PE = -\frac{GMm}{r}$$

$$\text{Total energy: } E = -\frac{GMm}{2r}$$

Centripetal Motion:

$$\text{Centripetal force: } F_c = \frac{mv^2}{r}$$

$$\text{Centripetal acceleration: } a_c = \frac{v^2}{r}$$

Physical Constants:

$$\text{Gravitational constant: } G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$$

$$\text{Earth's mass: } M_E = 5.97 \times 10^{24} \text{ kg}$$

$$\text{Earth's radius: } R_E = 6.37 \times 10^6 \text{ m}$$

$$\text{Moon's mass: } M_M = 7.35 \times 10^{22} \text{ kg}$$

$$\text{Moon's radius: } R_M = 1.74 \times 10^6 \text{ m}$$

$$\text{Acceleration due to gravity: } g = 9.81 \text{ m/s}^2$$

END OF TEST

Total marks: 210

Grade boundaries: A* 189, A 168, B 147, C 126, D 105, E 84

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