

# GCSE Foundation Mathematics

## Practice Test 3: Geometry and Measures

### Instructions:

Answer all questions. Show your working clearly.

Calculators may be used unless stated otherwise.

Time allowed: 90 minutes

### Section A: Angles

- Classify these angles as acute, obtuse, or reflex:
  - $38^\circ$
  - $145^\circ$
  - $315^\circ$
  - $89^\circ$
  - $205^\circ$
  - $12^\circ$
- Find the missing angles:
  - Two angles on a straight line are  $58^\circ$  and  $x^\circ$ . Find  $x$ .
  - Three angles around a point are  $105^\circ$ ,  $110^\circ$ , and  $y^\circ$ . Find  $y$ .
  - Two angles are vertically opposite. One angle is  $67^\circ$ . Find the other angle.
- In a triangle, two angles are  $48^\circ$  and  $85^\circ$ . Find the third angle.
- The angles in a triangle are in the ratio 3 : 4 : 5. Find the size of each angle.
- Find the missing angles in these triangles:
  - An isosceles triangle with base angles of  $x^\circ$  and vertex angle of  $30^\circ$
  - An equilateral triangle (all angles equal)
  - A right-angled triangle with one angle of  $58^\circ$

### Section B: Polygons and Angle Rules

- Find the sum of interior angles for:
  - A triangle (3 sides)
  - A hexagon (6 sides)
  - An octagon (8 sides)
  - An undecagon (11 sides)

7. Find the size of each interior angle in:
- (a) A regular pentagon
  - (b) A regular octagon
  - (c) A regular nonagon
  - (d) A regular hexagon
8. Find the size of each exterior angle in:
- (a) A regular pentagon
  - (b) A regular nonagon
  - (c) A regular decagon
  - (d) A regular hexagon
9. A regular polygon has an exterior angle of  $45^\circ$ . How many sides does it have?
10. In a quadrilateral, three angles are  $92^\circ$ ,  $88^\circ$ , and  $105^\circ$ . Find the fourth angle.
11. A regular polygon has an interior angle of  $135^\circ$ . Find:
- (a) The exterior angle
  - (b) The number of sides

## Section C: Properties of Shapes

12. State the properties of these quadrilaterals:
- (a) Parallelogram (sides, angles, diagonals)
  - (b) Trapezium (sides, angles)
  - (c) Rhombus (sides, angles, diagonals)
  - (d) Rectangle (sides, angles, diagonals)
13. How many lines of symmetry do these shapes have?
- (a) Regular hexagon
  - (b) Isosceles triangle
  - (c) Square
  - (d) Regular pentagon
  - (e) Rhombus
  - (f) Kite
14. What is the order of rotational symmetry for:
- (a) Regular octagon
  - (b) Equilateral triangle
  - (c) Square
  - (d) Rectangle
15. Name these 3D shapes:
- (a) 2 parallel circular faces and 1 curved surface
  - (b) 1 pentagonal base and 5 triangular faces
  - (c) 6 faces, all rectangles

- (d) 5 faces: 2 triangular and 3 rectangular
  - (e) 4 faces, all triangular
16. How many faces, edges, and vertices do these shapes have?
- (a) Cube
  - (b) Pentagonal pyramid
  - (c) Octagonal prism
  - (d) Triangular pyramid

## Section D: Transformations

17. Describe the transformation that maps:
- (a) Triangle A to Triangle B (reflection in line  $y = x$ )
  - (b) Triangle B to Triangle C (translation 2 units left, 4 units up)
  - (c) Triangle C to Triangle D (rotation  $180^\circ$  about origin)
  - (d) Triangle D to Triangle E (enlargement scale factor  $\frac{1}{2}$ , centre origin)
18. A point P(5, 3) is transformed. Find the image coordinates after:
- (a) Reflection in the x-axis
  - (b) Reflection in the y-axis
  - (c) Reflection in the line  $y = x$
  - (d) Translation by vector  $\begin{pmatrix} -4 \\ 1 \end{pmatrix}$
19. A triangle has vertices at A(1, 3), B(5, 3), and C(3, 7). Find the coordinates after:
- (a) Rotation  $180^\circ$  about the origin
  - (b) Enlargement scale factor  $\frac{1}{2}$ , centre origin
  - (c) Translation by vector  $\begin{pmatrix} 2 \\ -5 \end{pmatrix}$
20. A shape is enlarged by scale factor 4. If the original area is  $12 \text{ cm}^2$ , what is the new area?
21. Triangle A is enlarged to Triangle B with scale factor  $\frac{1}{2}$ . If Triangle A has a perimeter of 24 cm, what is the perimeter of Triangle B?

## Section E: Perimeter and Area

22. Calculate the perimeter of these shapes:
- (a) Rectangle: length 11 cm, width 7 cm
  - (b) Square: side length 9 cm
  - (c) Triangle: sides 7 cm, 9 cm, 11 cm
  - (d) Regular octagon: side length 5 cm
23. Calculate the area of these shapes:
- (a) Rectangle: length 14 cm, width 9 cm
  - (b) Square: side length 13 cm
  - (c) Triangle: base 16 cm, height 7 cm

- (d) Parallelogram: base 12 cm, height 8 cm
24. Calculate the area and circumference of circles with:
- (a) Radius 7 cm
  - (b) Diameter 12 cm
  - (c) Radius 2.5 cm
  - (d) Diameter 22 cm
25. A rectangular playground is 25 m long and 16 m wide. Find:
- (a) The perimeter
  - (b) The area
  - (c) The cost of fencing at £18 per metre
  - (d) The cost of artificial grass at £12 per  $\text{m}^2$
26. Find the area of these compound shapes:
- (a) A rectangle 14 cm by 9 cm with a square of side 4 cm removed from one corner
  - (b) An L-shape made from two rectangles: 12 cm by 5 cm and 8 cm by 6 cm
  - (c) A semicircle with radius 6 cm attached to a rectangle 12 cm by 8 cm

## Section F: Volume and Surface Area

27. Calculate the volume of these prisms:
- (a) Cuboid: length 10 cm, width 7 cm, height 6 cm
  - (b) Cube: side length 8 cm
  - (c) Triangular prism: triangular face area  $20 \text{ cm}^2$ , length 9 cm
  - (d) Cylinder: radius 5 cm, height 12 cm
28. Calculate the surface area of:
- (a) Cube: side length 7 cm
  - (b) Cuboid: length 12 cm, width 8 cm, height 6 cm
  - (c) Cylinder: radius 5 cm, height 8 cm
29. A cylindrical grain silo has radius 3 m and height 8 m. Find:
- (a) The volume in  $\text{m}^3$
  - (b) The volume in litres ( $1 \text{ m}^3 = 1000 \text{ litres}$ )
  - (c) The curved surface area
  - (d) The total surface area
30. A cube has volume  $343 \text{ cm}^3$ . Find:
- (a) The side length
  - (b) The surface area
31. A rectangular fish tank is 12 m long, 6 m wide, and 2.5 m deep. Find:
- (a) The volume of water needed to fill it
  - (b) The area of the bottom
  - (c) The area of the four walls

## Section G: Pythagoras' Theorem

32. Use Pythagoras' theorem to find the missing side in these right-angled triangles:
- (a) Two shorter sides are 6 cm and 8 cm. Find the hypotenuse.
  - (b) Hypotenuse is 15 cm, one side is 9 cm. Find the other side.
  - (c) Two shorter sides are 7 cm and 24 cm. Find the hypotenuse.
  - (d) Hypotenuse is 29 cm, one side is 21 cm. Find the other side.
33. A ladder of length 8 m leans against a wall. The bottom of the ladder is 3.5 m from the wall. How high up the wall does the ladder reach?
34. A rectangle has length 20 cm and width 15 cm. Find the length of its diagonal.
35. Find the distance between these pairs of points:
- (a) (0, 0) and (8, 6)
  - (b) (3, 1) and (9, 9)
  - (c) (-3, 4) and (2, 16)
36. A right-angled triangle has legs of length  $x$  cm and  $(x + 5)$  cm, and hypotenuse  $(x + 7)$  cm. Find the value of  $x$ .
37. Determine whether these triangles are right-angled:
- (a) Sides 9 cm, 12 cm, 15 cm
  - (b) Sides 8 cm, 17 cm, 19 cm
  - (c) Sides 20 cm, 21 cm, 29 cm
  - (d) Sides 11 cm, 60 cm, 61 cm

## Section H: Problem Solving

38. A circular fountain has radius 3 m. A border of width 1.5 m surrounds the fountain. Find:
- (a) The area of the fountain
  - (b) The area of the border
  - (c) The total area including the border
39. A regular decagon has perimeter 40 cm. Find:
- (a) The length of each side
  - (b) Each interior angle
  - (c) Each exterior angle
40. A cylindrical storage tank has radius 4 cm and height 15 cm. Find:
- (a) How much it can hold (volume)
  - (b) The area of metal needed to make it (surface area)
  - (c) The cost of metal at £0.025 per  $\text{cm}^2$
41. Triangle DEF is isosceles with  $DE = DF$ . Angle  $EDF = 35^\circ$ . Find angles DEF and DFE.
42. A square and a circle have the same perimeter. If the square has side length 12 cm, find the radius of the circle.

43. A triangle has vertices at  $A(3, 1)$ ,  $B(9, 1)$ , and  $C(6, 9)$ . Find:
- (a) The length of each side
  - (b) The perimeter
  - (c) The area
  - (d) Whether the triangle is right-angled
44. A cone has base radius 8 cm and slant height 17 cm. Find:
- (a) The vertical height
  - (b) The volume
  - (c) The curved surface area
45. The floor of a classroom is 9 m by 7 m. Square tiles of side 35 cm are used to cover the floor. How many tiles are needed?

**Answer Space**

Use this space for your working and answers.

**END OF TEST**

Total marks: 100

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[stepupmaths.co.uk](http://stepupmaths.co.uk)**