

GCSE Foundation Mathematics

Practice Test 7: Geometry and Measures

Instructions:

Answer all questions. Show your working clearly.

Calculators may be used unless stated otherwise.

Time allowed: 90 minutes

Section A: Angles

- Classify these angles as acute, obtuse, or reflex:
 - 68°
 - 152°
 - 284°
 - 29°
 - 203°
 - 89°
- Find the missing angles:
 - Two angles on a straight line are 127° and x° . Find x .
 - Three angles around a point are 145° , 92° , and y° . Find y .
 - Two angles are vertically opposite. One angle is 134° . Find the other angle.
- In a triangle, two angles are 39° and 82° . Find the third angle.
- The angles in a triangle are in the ratio 3 : 7 : 8. Find the size of each angle.
- Find the missing angles in these triangles:
 - An isosceles triangle with base angles of x° and vertex angle of 74°
 - An equilateral triangle (all angles equal)
 - A right-angled triangle with one angle of 23°

Section B: Polygons and Angle Rules

- Find the sum of interior angles for:
 - An octagon (8 sides)
 - A decagon (10 sides)
 - A dodecagon (12 sides)
 - A 15-sided polygon

7. Find the size of each interior angle in:
- (a) A regular octagon
 - (b) A regular decagon
 - (c) A regular 15-sided polygon
 - (d) A regular dodecagon
8. Find the size of each exterior angle in:
- (a) A regular octagon
 - (b) A regular decagon
 - (c) A regular 15-sided polygon
 - (d) A regular dodecagon
9. A regular polygon has an exterior angle of 24° . How many sides does it have?
10. In a quadrilateral, three angles are 73° , 118° , and 89° . Find the fourth angle.
11. A regular polygon has an interior angle of 162° . Find:
- (a) The exterior angle
 - (b) The number of sides

Section C: Properties of Shapes

12. State the properties of these quadrilaterals:
- (a) Kite (sides, angles)
 - (b) Square (sides, angles, diagonals)
 - (c) Rhombus (sides, angles, diagonals)
 - (d) Isosceles trapezium (sides, angles, diagonals)
13. How many lines of symmetry do these shapes have?
- (a) Regular decagon
 - (b) Rhombus
 - (c) Regular octagon
 - (d) Kite
 - (e) Isosceles triangle
 - (f) Regular hexagon
14. What is the order of rotational symmetry for:
- (a) Regular decagon
 - (b) Regular octagon
 - (c) Rhombus
 - (d) Isosceles triangle
15. Name these 3D shapes:
- (a) 1 octagonal base and 8 triangular faces
 - (b) 2 hexagonal faces and 6 rectangular faces
 - (c) 8 triangular faces meeting at vertices

- (d) 2 circular faces and 1 curved surface
 - (e) 5 rectangular faces and 2 triangular faces
16. How many faces, edges, and vertices do these shapes have?
- (a) Hexagonal prism
 - (b) Octagonal pyramid
 - (c) Icosahedron (20 triangular faces)
 - (d) Pentagonal prism

Section D: Transformations

17. Describe the transformation that maps:
- (a) Shape A to Shape B (enlargement scale factor $\frac{1}{3}$, centre origin)
 - (b) Shape B to Shape C (rotation 60° anticlockwise about origin)
 - (c) Shape C to Shape D (reflection in line $y = -2$)
 - (d) Shape D to Shape E (translation 8 units right, 6 units up)
18. A point P(12, 15) is transformed. Find the image coordinates after:
- (a) Reflection in the x-axis
 - (b) Reflection in the y-axis
 - (c) Reflection in the line $y = x$
 - (d) Translation by vector $\begin{pmatrix} -8 \\ 5 \end{pmatrix}$
19. A hexagon has vertices at A(6, 12), B(12, 12), C(15, 6), D(12, 0), E(6, 0), and F(3, 6). Find the coordinates after:
- (a) Rotation 90° anticlockwise about the origin
 - (b) Enlargement scale factor $\frac{2}{3}$, centre origin
 - (c) Translation by vector $\begin{pmatrix} -7 \\ 4 \end{pmatrix}$
20. A shape is enlarged by scale factor $\frac{4}{5}$. If the original area is 125 cm^2 , what is the new area?
21. Shape A is enlarged to Shape B with scale factor $\frac{2}{7}$. If Shape A has a perimeter of 91 cm, what is the perimeter of Shape B?

Section E: Perimeter and Area

22. Calculate the perimeter of these shapes:
- (a) Rectangle: length 29 cm, width 16 cm
 - (b) Square: side length 22 cm
 - (c) Triangle: sides 19 cm, 21 cm, 25 cm
 - (d) Regular octagon: side length 9 cm
23. Calculate the area of these shapes:
- (a) Rectangle: length 31 cm, width 18 cm
 - (b) Square: side length 24 cm

- (c) Triangle: base 32 cm, height 15 cm
 - (d) Parallelogram: base 23 cm, height 12 cm
24. Calculate the area and circumference of circles with:
- (a) Radius 13 cm
 - (b) Diameter 28 cm
 - (c) Radius 9.5 cm
 - (d) Diameter 38 cm
25. A rectangular sports field is 85 m long and 52 m wide. Find:
- (a) The perimeter
 - (b) The area
 - (c) The cost of boundary fencing at £42 per metre
 - (d) The cost of grass seeding at £8 per m²
26. Find the area of these compound shapes:
- (a) A rectangle 28 cm by 18 cm with two squares of side 4 cm removed from opposite corners
 - (b) A plus sign made from two rectangles: 24 cm by 8 cm and 10 cm by 22 cm overlapping
 - (c) Two-thirds of a circle with radius 12 cm attached to a triangle with base 24 cm and height 18 cm

Section F: Volume and Surface Area

27. Calculate the volume of these prisms:
- (a) Cuboid: length 22 cm, width 15 cm, height 12 cm
 - (b) Cube: side length 14 cm
 - (c) Triangular prism: triangular face area 48 cm², length 16 cm
 - (d) Cylinder: radius 11 cm, height 18 cm
28. Calculate the surface area of:
- (a) Cube: side length 15 cm
 - (b) Cuboid: length 24 cm, width 18 cm, height 13 cm
 - (c) Cylinder: radius 10 cm, height 17 cm
29. A cylindrical water tank has radius 8 m and height 15 m. Find:
- (a) The volume in m³
 - (b) The volume in litres (1 m³ = 1000 litres)
 - (c) The curved surface area
 - (d) The total surface area
30. A cube has volume 2744 cm³. Find:
- (a) The side length
 - (b) The surface area
31. A rectangular warehouse is 45 m long, 22 m wide, and 6 m high. Find:
- (a) The volume of goods it can store
 - (b) The area of the floor
 - (c) The area of the four walls

Section G: Pythagoras' Theorem

32. Use Pythagoras' theorem to find the missing side in these right-angled triangles:
- (a) Two shorter sides are 24 cm and 32 cm. Find the hypotenuse.
 - (b) Hypotenuse is 65 cm, one side is 63 cm. Find the other side.
 - (c) Two shorter sides are 36 cm and 48 cm. Find the hypotenuse.
 - (d) Hypotenuse is 97 cm, one side is 72 cm. Find the other side.
33. A ladder of length 15 m is placed against a wall. The foot of the ladder is 9 m from the base of the wall. How high up the wall does the ladder reach?
34. A rectangle has length 52 cm and width 16 cm. Find the length of its diagonal.
35. Find the distance between these pairs of points:
- (a) (0, 0) and (24, 32)
 - (b) (8, 13) and (20, 18)
 - (c) (-6, 9) and (6, 24)
36. A right-angled triangle has legs of length x cm and $(x + 13)$ cm, and hypotenuse $(x + 67)$ cm. Find the value of x .
37. Determine whether these triangles are right-angled:
- (a) Sides 24 cm, 70 cm, 74 cm
 - (b) Sides 20 cm, 48 cm, 52 cm
 - (c) Sides 42 cm, 56 cm, 70 cm
 - (d) Sides 39 cm, 52 cm, 65 cm

Section H: Problem Solving

38. A circular garden has radius 14 m. A pathway of width 3 m surrounds the garden. Find:
- (a) The area of the garden
 - (b) The area of the pathway
 - (c) The total area including the pathway
39. A regular 20-sided polygon has perimeter 140 cm. Find:
- (a) The length of each side
 - (b) Each interior angle
 - (c) Each exterior angle
40. A cylindrical oil tank has radius 13 cm and height 35 cm. Find:
- (a) How much oil it can store (volume)
 - (b) The area of metal needed to construct it (surface area)
 - (c) The cost of metal at £0.12 per cm^2
41. Triangle PQR is isosceles with $PQ = PR$. Angle $QPR = 18^\circ$. Find angles PQR and PRQ.
42. A regular hexagon and a circle have the same area. If the hexagon has side length 12 cm, find the radius of the circle (use hexagon area $= \frac{3\sqrt{3}}{2} \times \text{side}^2$).

43. A triangle has vertices at A(8, 12), B(20, 12), and C(14, 27). Find:
- (a) The length of each side
 - (b) The perimeter
 - (c) The area
 - (d) Whether the triangle is right-angled
44. A cone has base radius 18 cm and slant height 30 cm. Find:
- (a) The vertical height
 - (b) The volume
 - (c) The curved surface area
45. A swimming pool area is 25 m by 18 m. Octagonal tiles with side length 30 cm are used around the pool edge. Approximately how many tiles are needed for a 2 m wide border? (Use octagon area $4.8 \times \text{side}^2$)

Answer Space

Use this space for your working and answers.

END OF TEST

Total marks: 100

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