

# A Level Mechanics

## Practice Test 3: Kinematics

### Instructions:

Answer all questions. Show your working clearly.

Calculators may be used unless stated otherwise.

Draw diagrams where appropriate to illustrate your solutions.

Time allowed: 2 hours 40 minutes

### Section A: Advanced Mathematical Motion [30 marks]

**Question 1 [18 marks]** A particle moves along a straight line such that its acceleration at time  $t$  seconds is given by  $a = 6t - 18$  m/s<sup>2</sup>. At  $t = 0$ , the particle has velocity 10 m/s and is at position  $s = 5$  m.

- (a) Find the velocity of the particle at time  $t$ . [4 marks]
- (b) Determine the position of the particle at time  $t$ . [4 marks]
- (c) Calculate when the particle is momentarily at rest. [3 marks]
- (d) Find the position of the particle when it is at rest. [2 marks]
- (e) Determine when the acceleration is zero. [2 marks]
- (f) Calculate the total distance traveled between  $t = 0$  and  $t = 6$  seconds. [3 marks]

**Question 2 [12 marks]** The displacement-time graph of a particle shows the following motion over 10 seconds: - Starts at  $s = 0$  - Increases linearly to  $s = 20$  m at  $t = 4$  s - Remains constant at  $s = 20$  m from  $t = 4$  s to  $t = 7$  s - Decreases linearly to  $s = 8$  m at  $t = 10$  s

- (a) Sketch the corresponding velocity-time graph. [4 marks]
- (b) Calculate the velocity during each phase of motion. [3 marks]
- (c) Determine the average velocity over the entire 10 seconds. [2 marks]
- (d) Calculate the total distance traveled. [3 marks]

### Section B: Multi-Stage Motion Analysis [35 marks]

**Question 3 [20 marks]** A train journey consists of four stages: 1. Accelerates from rest at 0.8 m/s<sup>2</sup> for 30 seconds 2. Travels at constant speed for 5 minutes 3. Decelerates at 0.6 m/s<sup>2</sup> for 40 seconds 4. Travels at the new constant speed for 3 minutes

- (a) Calculate the speed reached after stage 1. [2 marks]
- (b) Find the distance covered in stage 1. [3 marks]

- (c) Calculate the distance covered in stage 2. [2 marks]
- (d) Determine the final speed after stage 3. [3 marks]
- (e) Find the distance covered in stage 3. [3 marks]
- (f) Calculate the distance covered in stage 4. [2 marks]
- (g) Determine the total distance for the entire journey. [2 marks]
- (h) Calculate the average speed for the entire journey. [3 marks]

**Question 4 [15 marks]** Two particles A and B start from the same point at  $t = 0$ . Particle A moves with constant velocity 12 m/s. Particle B starts from rest and accelerates at  $1.5 \text{ m/s}^2$  for 10 seconds, then moves with constant velocity.

- (a) Write displacement equations for both particles for  $t \leq 10 \text{ s}$ . [3 marks]
- (b) Find when particle A is furthest ahead of particle B during the first 10 seconds. [4 marks]
- (c) Calculate the maximum separation between the particles. [3 marks]
- (d) Determine when particle B catches up with particle A. [5 marks]

## Section C: Vertical Motion and Collision Analysis [30 marks]

**Question 5 [18 marks]** From the top of a tower 60 m high, one ball is dropped while another is thrown vertically downward with initial velocity 8 m/s. Both balls are released simultaneously.

- (a) Write height equations for both balls. [4 marks]
- (b) Calculate when each ball hits the ground. [6 marks]
- (c) Find the velocities of both balls just before impact. [4 marks]
- (d) Determine the vertical separation between the balls after 2 seconds. [4 marks]

**Question 6 [12 marks]** A ball is thrown vertically upward from ground level. It passes a window 15 m above the ground twice - once on the way up after 1.5 seconds, and once on the way down.

- (a) Calculate the initial velocity of the ball. [4 marks]
- (b) Find the maximum height reached by the ball. [3 marks]
- (c) Determine when the ball passes the window on the way down. [3 marks]
- (d) Calculate the total time of flight. [2 marks]

## Section D: Complex Inclined Plane Motion [25 marks]

**Question 7 [15 marks]** A particle slides up a smooth inclined plane that makes an angle of  $18^\circ$  with the horizontal. The particle has an initial velocity of 16 m/s up the plane.

- (a) Calculate the deceleration of the particle up the plane. [3 marks]
- (b) Find how far up the plane the particle travels before coming to rest. [4 marks]
- (c) Calculate the time taken to reach the highest point. [3 marks]
- (d) Determine the particle's velocity after sliding back down for 3 seconds. [3 marks]

- (e) Find the particle's position relative to its starting point after 8 seconds total. [2 marks]

**Question 8 [10 marks]** A block is placed on an inclined plane  $25^\circ$  to the horizontal. Due to friction, the block accelerates down the plane at  $2.8 \text{ m/s}^2$  when released from rest.

- (a) Calculate the coefficient of friction between the block and plane. [5 marks]  
(b) If the plane is 10 m long, find the speed at the bottom. [3 marks]  
(c) Calculate the time taken to reach the bottom. [2 marks]

## Section E: Advanced Projectile Motion [40 marks]

**Question 9 [25 marks]** A golf ball is hit from ground level with initial velocity  $45 \text{ m/s}$  at an angle of  $25^\circ$  above the horizontal. The ball lands on a green that is 8 m above the level of the tee.

- (a) Calculate the horizontal and vertical components of initial velocity. [3 marks]  
(b) Write parametric equations for the ball's position. [3 marks]  
(c) Find the time when the ball reaches its maximum height. [3 marks]  
(d) Calculate the maximum height above the tee level. [3 marks]  
(e) Determine the two times when the ball is at height 8 m above the tee. [6 marks]  
(f) Calculate the horizontal distances for both times in part (e). [4 marks]  
(g) Find the velocity components when the ball first reaches the green level. [3 marks]

**Question 10 [15 marks]** A projectile is launched from the edge of a cliff 35 m high with initial velocity  $24 \text{ m/s}$  at  $50^\circ$  below the horizontal.

- (a) Calculate the horizontal and vertical components of initial velocity. [3 marks]  
(b) Write equations for the projectile's position. [3 marks]  
(c) Find when the projectile hits the ground. [4 marks]  
(d) Calculate the horizontal distance from the cliff base where it lands. [2 marks]  
(e) Determine the velocity components just before impact. [3 marks]

## Section F: Vector Motion and Relative Velocity [25 marks]

**Question 11 [15 marks]** Ship A is traveling due east at  $15 \text{ m/s}$  while ship B is traveling northwest at  $12 \text{ m/s}$ . At  $t = 0$ , ship A is at the origin and ship B is at position (800 m, 600 m).

- (a) Write position vector equations for both ships. [4 marks]  
(b) Calculate the velocity of ship B relative to ship A. [4 marks]  
(c) Find when the ships are closest together. [4 marks]  
(d) Determine the minimum distance between the ships. [3 marks]

**Question 12 [10 marks]** A pilot wants to fly from airport A to airport B, which is 200 km due north of A. The aircraft's airspeed is  $180 \text{ km/h}$  and there is a wind of  $40 \text{ km/h}$  from the west.

- (a) In what direction should the pilot head to fly directly from A to B? [4 marks]

- (b) Calculate the ground speed for this direct flight. [3 marks]
- (c) Find the time taken for the journey. [2 marks]
- (d) If the pilot heads due north instead, how far east of airport B will the aircraft be after flying for the same time? [1 mark]

## Section G: Comprehensive Motion Problems [25 marks]

**Question 13 [25 marks]** A ball is thrown from point A on the ground with velocity 20 m/s at  $60^\circ$  to the horizontal. At the same instant, another ball is thrown vertically upward from point B (which is 25 m horizontally from A) with initial velocity 18 m/s.

- (a) Write position equations for both balls. [4 marks]
- (b) Calculate when ball A reaches its maximum height. [2 marks]
- (c) Find the maximum height reached by ball A. [3 marks]
- (d) Determine when ball B reaches its maximum height. [2 marks]
- (e) Calculate the maximum height reached by ball B. [3 marks]
- (f) Find if and when the balls are at the same height. [5 marks]
- (g) Calculate the horizontal separation between the balls when they are at the same height. [3 marks]
- (h) Determine which ball hits the ground first and by how much time. [3 marks]

### Physics Data and Formulae

#### Calculus and Motion:

$$v = \frac{ds}{dt}, a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$v = \int a \, dt + C, s = \int v \, dt + C$$

#### SUVAT Equations:

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

$$s = \frac{u+v}{2}t$$

$$s = vt - \frac{1}{2}at^2$$

#### Projectile Motion:

Horizontal:  $x = x_0 + u_x t$  (where  $u_x = u \cos \theta$ )

Vertical:  $y = y_0 + u_y t - \frac{1}{2}gt^2$  (where  $u_y = u \sin \theta$ )

Velocity components:  $v_x = u_x, v_y = u_y - gt$

Resultant velocity:  $v = \sqrt{v_x^2 + v_y^2}$

Direction:  $\tan \alpha = \frac{v_y}{v_x}$

#### Inclined Plane Motion:

Component down plane:  $mg \sin \theta - \mu mg \cos \theta = ma$

For smooth plane:  $a = g \sin \theta$

With friction:  $a = g(\sin \theta - \mu \cos \theta)$

**Vector Analysis:**

Position vector:  $\vec{r} = x\hat{i} + y\hat{j}$

Velocity vector:  $\vec{v} = \frac{d\vec{r}}{dt}$

Relative velocity:  $\vec{v}_{AB} = \vec{v}_A - \vec{v}_B$

Magnitude:  $|\vec{v}| = \sqrt{v_x^2 + v_y^2}$

**Constants:**

Acceleration due to gravity:  $g = 9.8 \text{ m/s}^2$

**Trigonometric Values:**

$\sin 18 = 0.309, \cos 18 = 0.951$

$\sin 25 = 0.423, \cos 25 = 0.906$

$\sin 50 = 0.766, \cos 50 = 0.643$

$\sin 60 = 0.866, \cos 60 = 0.500$

$\sin 45 = 0.707, \cos 45 = 0.707$  (for northwest direction)

**END OF TEST**

Total marks: 210

Grade boundaries: A\* 189, A 168, B 147, C 126, D 105, E 84

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**[stepupmaths.co.uk](http://stepupmaths.co.uk)**